

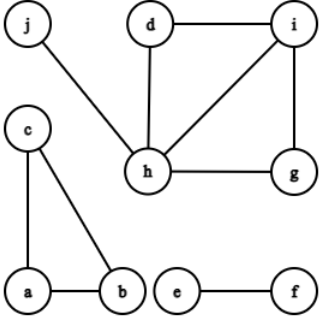
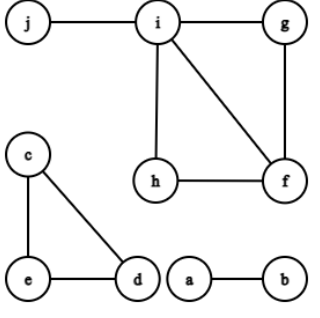
pembahasan trial uas diskrit 2023

(lebih ke jawaban sih)



disusun oleh:

the one and only @kafeyangasli

SOAL A  
1. GRAF

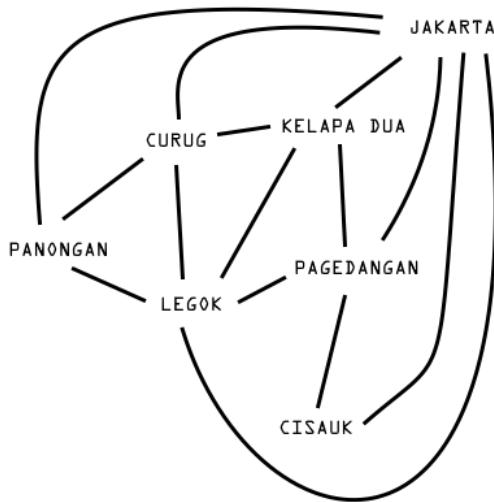
|  |   |  |  |
|--|---|--|--|
| <b>NIM GANJIL</b>  |   | <b>NIM GENAP</b>   |  |
| $V = \{a, b, c, d, e, f, g, h, i, j\}$<br>$E = \{(a, b), (b, c), (a, c), (e, f), (d, i), (d, h), (h, j), (h, i), (g, h), (g, i)\}$ |   | $V = \{a, b, c, d, e, f, g, h, i, j\}$<br>$E = \{(a, b), (c, d), (c, e), (d, e), (f, g), (f, i), (f, h), (g, i), (i, h), (i, j)\}$ |  |
| Gambar Graf (A)  |    | Gambar Graf (A)  |   |
| Apakah graf G merupakan graf terhubung? (B)  | Graf G <b>bukanlah</b> graf terhubung, karena graf G memiliki tiga komponen yang terpisah tanpa ada sisi yang menghubungkan komponen-komponen tersebut. |  |  |
| Derajat (C)  | $D(a) = 2$<br>$D(b) = 2$<br>$D(c) = 2$<br>$D(d) = 2$<br>$D(e) = 1$<br>$D(f) = 1$<br>$D(g) = 2$<br>$D(h) = 4$<br>$D(i) = 3$<br>$D(j) = 1$                | Derajat (C)  | $D(a) = 1$<br>$D(b) = 1$<br>$D(c) = 2$<br>$D(d) = 2$<br>$D(e) = 2$<br>$D(f) = 2$<br>$D(g) = 2$<br>$D(h) = 3$<br>$D(i) = 4$<br>$D(j) = 1$ |

SOAL B  
1. WELCH-POWELL ALGORITHM

|   |  |
|---|--|
| <b>NIM GANJIL</b>   | <b>NIM GENAP</b>   |
|  |  |

\*asumsikan daerah luar sebagai JAKARTA

a. Graf Dualnya adalah sebagai berikut:



b. Pewarnaan Bidang dengan Welch-Powell

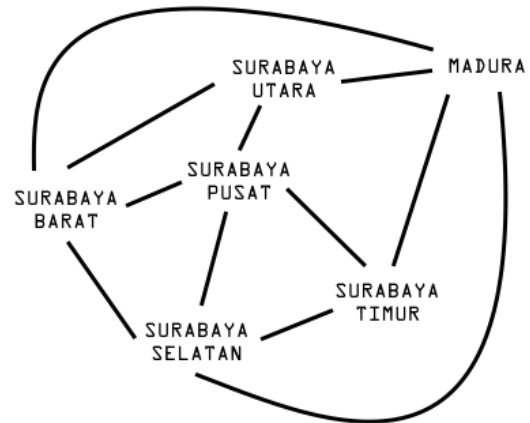
| Vertex | JK | LE | PG | KD | CG | PN | CS |
|--------|----|----|----|----|----|----|----|
| Degree | 6  | 5  | 4  | 4  | 4  | 3  | 2  |
| Colour | M  | B  | H  | K  | H  | K  | B  |

c. Bilangan Kromatik

$$\chi(G_{\text{ganjil}}) = 4$$

\*asumsikan daerah luar sebagai MADURA

a. Graf Dualnya adalah sebagai berikut:



b. Pewarnaan Bidang dengan Welch-Powell

| Vertex | MD | SB | SP | SS | ST | SU |
|--------|----|----|----|----|----|----|
| Degree | 4  | 4  | 4  | 4  | 3  | 3  |
| Colour | M  | B  | M  | H  | B  | H  |

c. Bilangan Kromatik

$$\chi(G_{\text{genap}}) = 3$$

## 2. HUFFMAN COMPRESSION

### NIM GANJIL

Data Frekuensi

| Karakter  | P | A | C | F  | K | U | N  |
|-----------|---|---|---|----|---|---|----|
| Frekuensi | 8 | 3 | 7 | 10 | 6 | 1 | 15 |

a. Pohon Huffman yang terbentuk

#### ITERASI PERTAMA

|   |   |   |   |   |    |    |
|---|---|---|---|---|----|----|
| U | A | K | C | P | F  | N  |
| 1 | 3 | 6 | 7 | 8 | 10 | 15 |

#### ITERASI KEDUA

|     |   |   |   |    |    |
|-----|---|---|---|----|----|
| 4   | K | C | P | F  | N  |
| U A | 6 | 7 | 8 | 10 | 15 |

#### ITERASI KETIGA

|   |   |       |    |    |
|---|---|-------|----|----|
| C | P | 10    | F  | N  |
| 7 | 8 | 4 K   | 10 | 15 |
|   |   | U A 6 |    |    |

### NIM GANJIL

Data Frekuensi

| Karakter  | M | D  | A | C | T | S | B  |
|-----------|---|----|---|---|---|---|----|
| Frekuensi | 6 | 10 | 3 | 7 | 5 | 2 | 17 |

a. Pohon Huffman yang terbentuk

#### ITERASI PERTAMA

|   |   |   |   |   |    |    |
|---|---|---|---|---|----|----|
| S | A | T | M | C | D  | B  |
| 2 | 3 | 5 | 6 | 7 | 10 | 17 |

#### ITERASI KEDUA

|     |   |   |   |    |    |
|-----|---|---|---|----|----|
| 5   | T | M | C | D  | B  |
| S A | 5 | 6 | 7 | 10 | 17 |

#### ITERASI KETIGA

|   |   |       |    |    |
|---|---|-------|----|----|
| M | C | 10    | D  | B  |
| 6 | 7 | 5 T   | 10 | 17 |
|   |   | S A 5 |    |    |

**ITERASI KEEMPAT**

|       |    |     |    |
|-------|----|-----|----|
| 10    | F  | 15  | N  |
| 4 K   | 10 | C P | 15 |
| U A 6 |    | 7 8 |    |

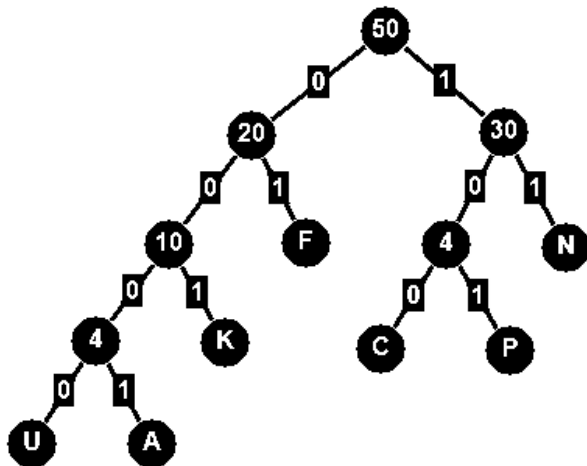
**ITERASI KELIMA**

|     |    |        |
|-----|----|--------|
| 15  | N  | 20     |
| C P | 15 | 10 F   |
| 7 8 |    | 4 K 10 |
|     |    | U A 6  |

**ITERASI KEENAM**

|        |        |
|--------|--------|
| 20     | 30     |
| 10 F   | 15 N   |
| 4 K 10 | C P 15 |
| U A 6  | 7 8    |

**POHON HUFFMAN**



**ITERASI KEEMPAT**

|       |    |     |    |
|-------|----|-----|----|
| 10    | D  | 13  | B  |
| 5 T   | 10 | M C | 17 |
| S A 5 |    | 6 7 |    |

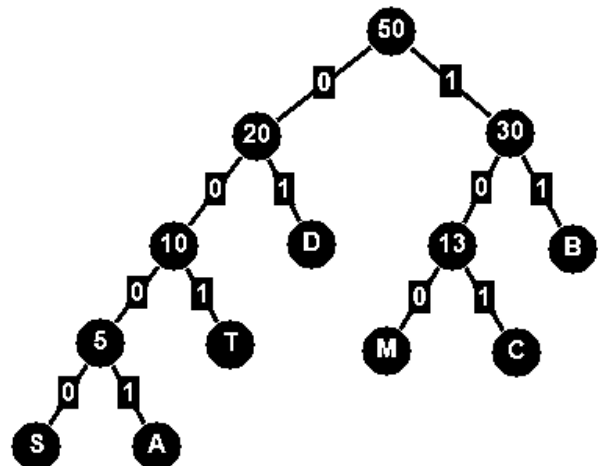
**ITERASI KELIMA**

|     |    |        |
|-----|----|--------|
| 13  | B  | 20     |
| M C | 17 | 10 D   |
| 6 7 |    | 5 T 10 |
|     |    | S A 5  |

**ITERASI KEENAM**

|        |        |
|--------|--------|
| 20     | 30     |
| 10 D   | 13 B   |
| 5 T 10 | M C 17 |
| S A 5  | 6 7    |

**POHON HUFFMAN**



b. Kode Biner Data

|   |      |
|---|------|
| N | 11   |
| F | 01   |
| K | 001  |
| C | 100  |
| P | 101  |
| U | 0000 |
| A | 0001 |

c. Rasio Kompresi

*Original* = 50 × 8 = 400 bit

*Huffman* = 30 + 20 + 18 + 21 + 24 + 4 + 12  
= 129 bit

*Rasio* =  $(1 - \frac{129}{400}) \times 100$   
≈ 67,75%

b. Kode Biner Data

|   |      |
|---|------|
| B | 11   |
| D | 01   |
| T | 001  |
| M | 100  |
| C | 101  |
| S | 0000 |
| A | 0001 |

c. Rasio Kompresi

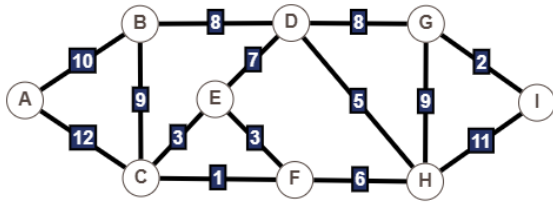
*Original* = 50 × 8 = 400 bit

*Huffman* = 34 + 20 + 15 + 18 + 21 + 8 + 12  
= 128 bit

*Rasio* =  $(1 - \frac{128}{400}) \times 100$   
≈ 68%

### 3. SHORTEST PATH & MINIMUM SPANNING TREE

#### NIM GANJIL



<https://graphonline.top/en/?graph=hEONfDCoqarpTkSZZcst>  
 \*dikarenakan keambiguan soal, sisi DF dianggap tidak ada

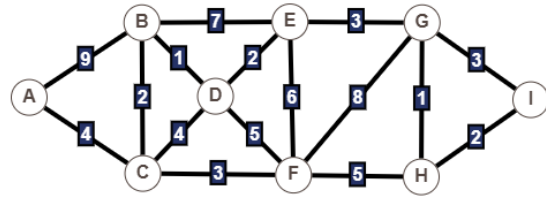
#### a. Dijkstra Algorithm

|   | A  | B   | C   | D   | E   | F   | G   | H   | I   |
|---|----|-----|-----|-----|-----|-----|-----|-----|-----|
| A | ∞A | 10A | 12A | XX  | XX  | XX  | XX  | XX  | XX  |
| B |    |     | 12A | 18B | XX  | XX  | XX  | XX  | XX  |
| C |    |     |     | 18B | 15C | 13C | XX  | XX  | XX  |
| F |    |     |     | 18B | 15C |     | XX  | 19F | XX  |
| E |    |     |     | 18B |     |     | XX  | 19F | XX  |
| D |    |     |     |     |     |     | 26D | 19F | XX  |
| H |    |     |     |     |     |     | 26D |     | 30H |
| G |    |     |     |     |     |     |     |     | 28G |

Shortest Path from A to:

- B : A → B
- C : A → C
- D : A → B → D
- E : A → C → E
- F : A → C → F
- G : A → B → D → G
- H : A → C → F → H
- I : A → B → D → G → I

#### NIM GENAP



<https://graphonline.top/en/?graph=BAYYXOVNUchpVwDiZZcst>

#### a. Dijkstra Algorithm

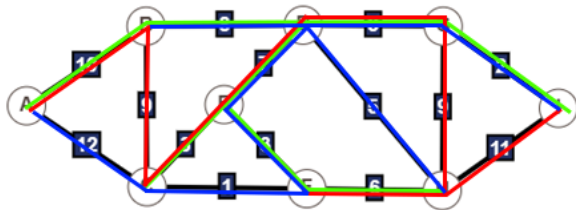
|   | A  | B  | C  | D  | E   | F  | G   | H   | I   |
|---|----|----|----|----|-----|----|-----|-----|-----|
| A | ∞A | 9A | 4C | XX | XX  | XX | XX  | XX  | XX  |
| C |    | 6C |    | 8C | XX  | 7C | XX  | XX  | XX  |
| B |    |    |    | 7B | 13B | 7C | XX  | XX  | XX  |
| D |    |    |    |    | 9D  | 7C | XX  | XX  | XX  |
| F |    |    |    |    | 9D  |    | 15F | 12F | XX  |
| E |    |    |    |    |     |    | 12E | 12F | XX  |
| G |    |    |    |    |     |    |     | 12F | 15G |
| H |    |    |    |    |     |    |     |     | 14H |

Shortest Path from A to:

- B : A → C → B
- C : A → C
- D : A → C → B → D
- E : A → C → B → D → E
- F : A → C → F
- G : A → C → B → D → E → G
- H : A → C → F → H
- I : A → C → F → H → I

#### b. Tiga Spanning Tree

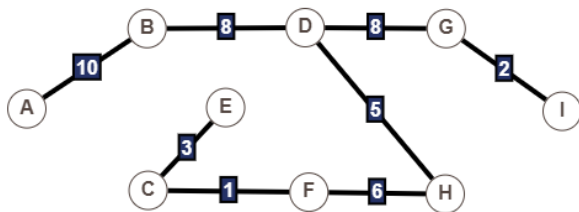
(bisa bervariasi, tidak harus persis seperti dibawah)



\*setiap warna merepresentasikan satu spanning tree, karena saya malas menggambar ulang

#### c. Minimum Spanning Tree

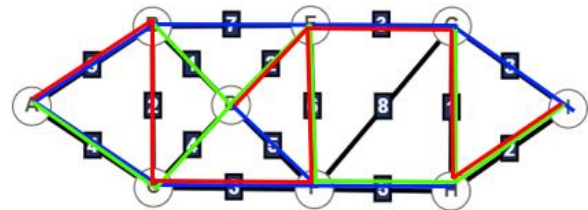
(Total Derajat = 43):



\*tidak unik, CE bisa diganti dengan EF

#### b. Tiga Spanning Tree

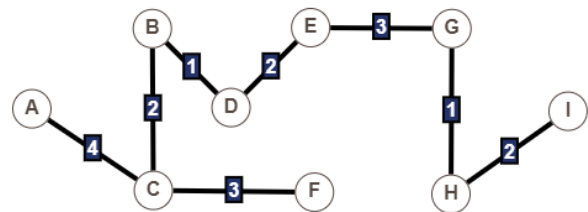
(bisa bervariasi, tidak harus persis seperti dibawah)



\*setiap warna merepresentasikan satu spanning tree, karena saya malas menggambar ulang

#### c. Minimum Spanning Tree

(Total Derajat = 18):



Proses Algoritma Kruskal:

| Node | Degree |
|------|--------|
| CF   | 1      |
| GI   | 2      |
| CE   | 3      |
| EF   | 3      |
| DH   | 5      |
| FH   | 6      |
| ED   | 7      |
| BD   | 8      |
| DG   | 8      |
| BC   | 9      |
| GH   | 9      |
| AB   | 10     |
| HI   | 11     |
| AC   | 12     |

Proses Algoritma Kruskal:

| Node | Degree |
|------|--------|
| BD   | 1      |
| GH   | 1      |
| BC   | 2      |
| DE   | 2      |
| HI   | 2      |
| EG   | 3      |
| GI   | 3      |
| CF   | 3      |
| AC   | 4      |
| CD   | 4      |
| DF   | 5      |
| FH   | 5      |
| EF   | 6      |
| BE   | 7      |
| FG   | 8      |
| AB   | 9      |